

How to model the positioning error

High Quality Positioning:
a Key to Success for
Autonomous Driving

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Ifsttar

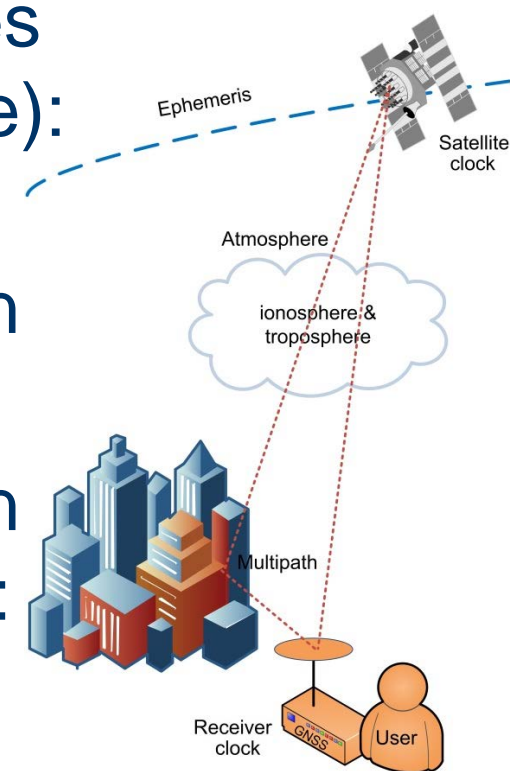
Abstract (3 subsections)

- Error sources and influencing parameters
- Learning process based on field testing
- Error modeling and simulation, and validation



Error sources (1st §)

- Errors originating from the satellites (to which one measures a distance): clocks, orbits
- Errors originating from propagation through atmosphere: iono, tropo
- Errors originating from propagation locally at receiver level (multipath): malicious attacks not being considered here



Typical error standard deviations

Source	Range error (standard deviation, 1 sigma)
Residual satellite ephemeris and clock errors	0.5 m
Residual ionosphere error (single-frequency)	4.0 m
Residual ionosphere error (dual-frequency)	0.1 m
Residual troposphere error (assuming latitude and season dependent model)	0.2 m
Multipath error for code meas. (~100 x less for phase)	=> Several tens of m
Tracking noise for code meas. (~100 x less for phase)	< 1.0 m

- Multipath error have non random nature: bias and possibly 3D modeled

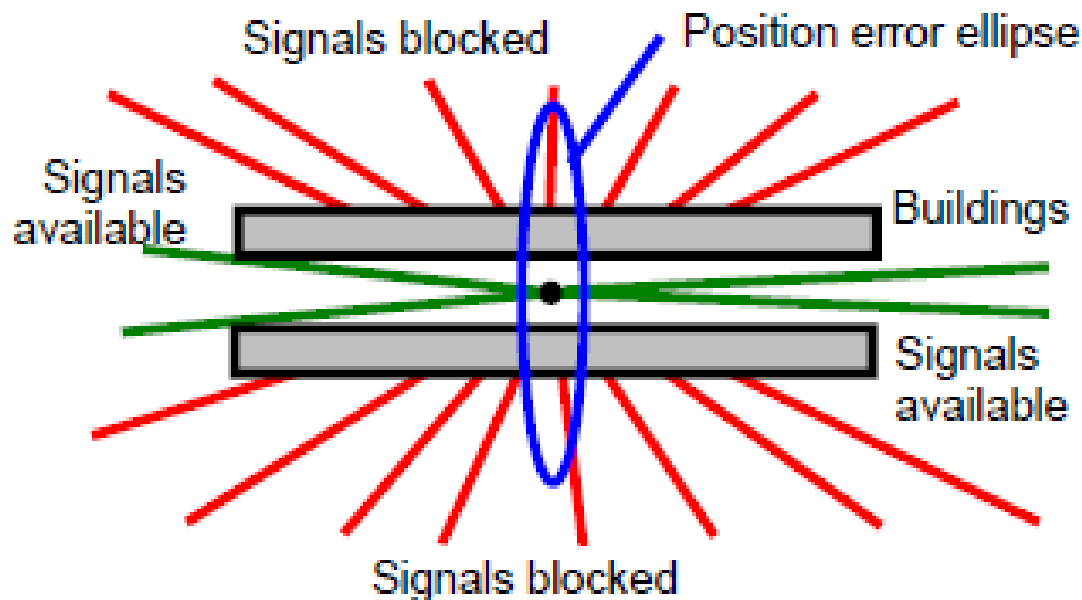
Last, but not least, system DOP

- Even if no bias would impact ranging...
- Ranging noise to positioning noise statistics through the mathematics of trilateration
- Non isotropic error (lat / lon / alt)
- DOP, system coverage, Earth poles issue
- Street along / cross errors satellite geometry



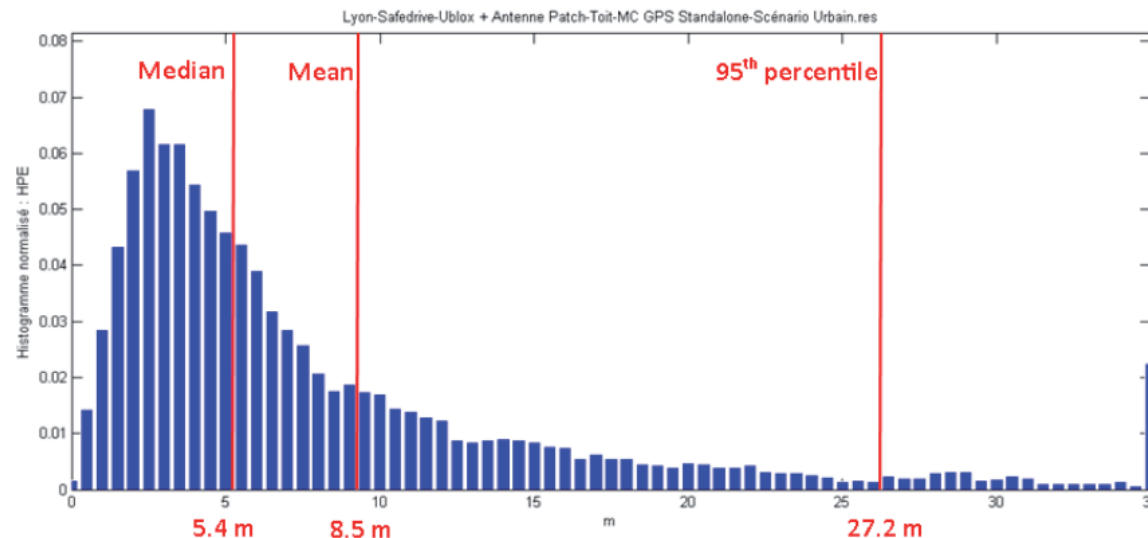
Non isotropic error in urban GNSS

- From Paul Groves' IUP (Intelligent Urban Positioning)



Influencing parameters

- MAIN error source due to MULTIPATH
- Local obstacles, buildings, foliage, vehicle itself (windshield vs roof antenna placing)
- Non Line Of Sight satellite tracking leads to significant tail position error distribution



Source: M3 Systems, EGNOS on the road, 2009



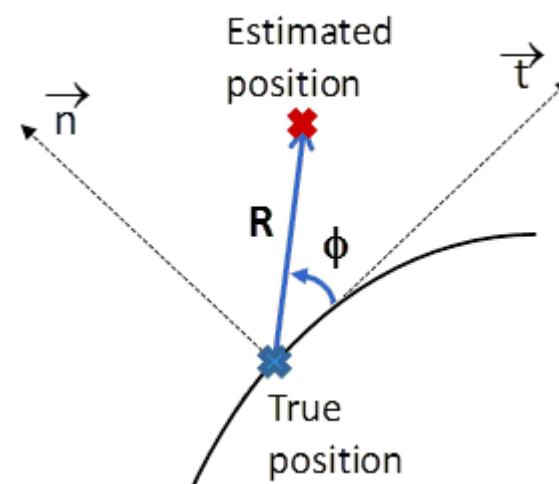
Field testing (2nd §)

- Every GNSS terminal model being specific... one needs to experiment
- Similar using conditions lead to receiver (hw and sw) dependent performance
- Testing campaign



Reference trajectory

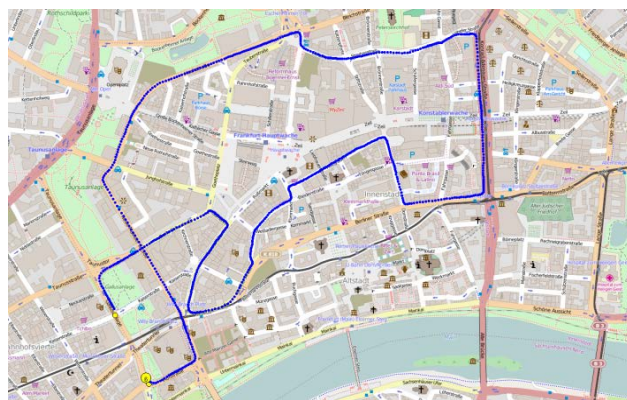
- Field testing is based on a time-to-time difference between positions provided by:
 - the equipment under investigation and
 - a reference system (e.g. Ifsttar VERT)



Positioning error characterization

- Error time series
- Distribution
- Auto-correlation

Illustration: QFree tests in Frankfurt 5km in deep urban canyons with dense traffic 15kph

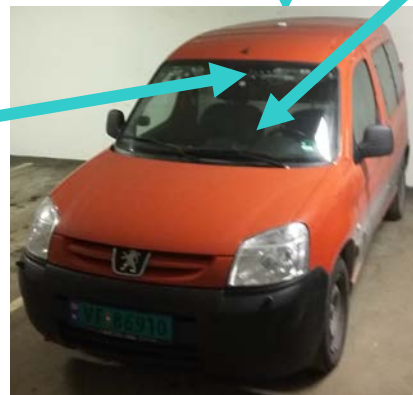


Ground truth GNSS-aided
Inertial Navigation System

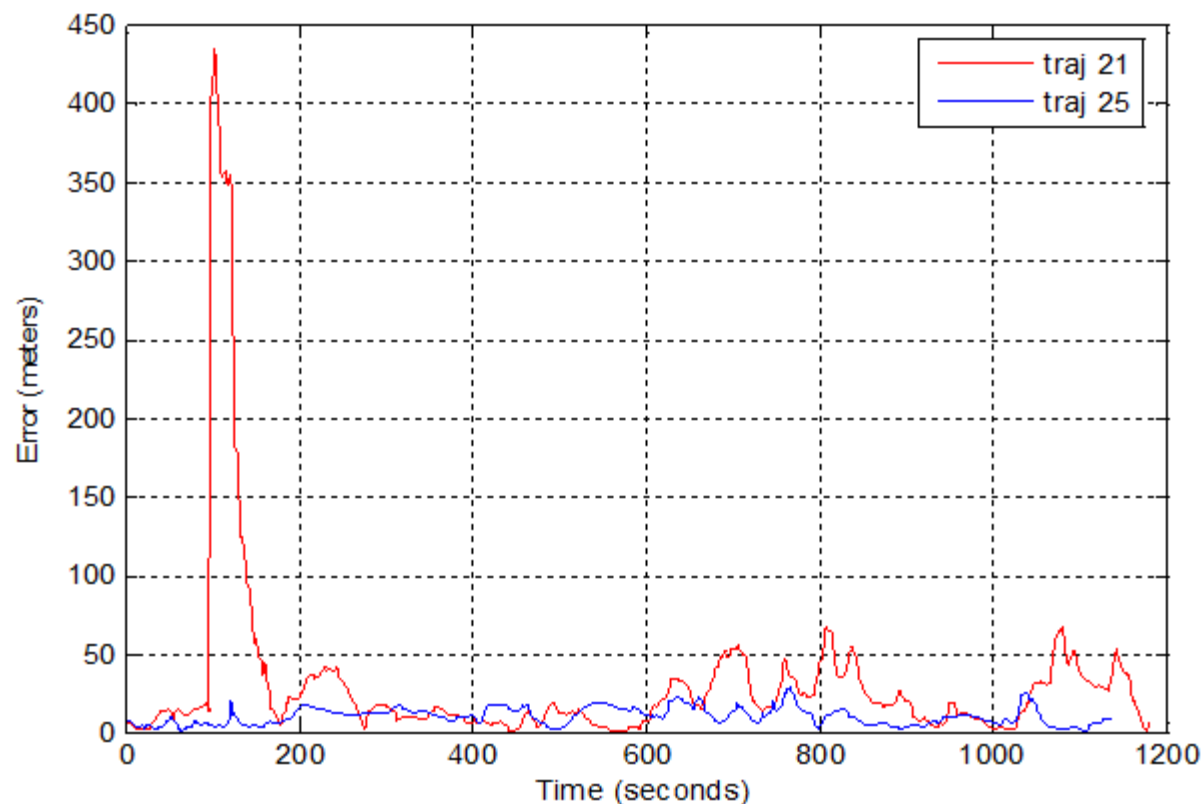
Ground truth antenna

Automotive
GNSS antenna
and receiver
in test

Rx considered:
uBlox LEA5-T.



Position error of best & worst trajectories (/ 28 loops)



Error modeling & simulation (3rd §)

- For large testing applications based on positioning
- Simulation of non Gaussian distributed error with dynamic (and not only static) shaping in order to make trajectory error cloning

Positioning error simulation

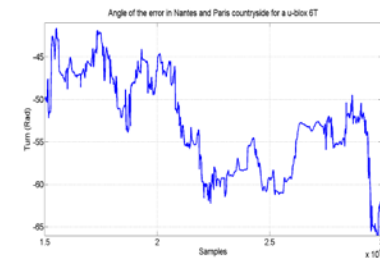
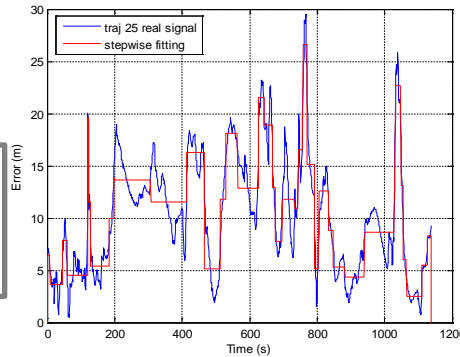
- In quite nice environment, despite it makes non ergodic non stationary error, a simple AR model is convenient (by Telespazio in GP-Start): $\text{error}_k = a * \text{error}_{k-1} + \text{noise}_k$
- If large NLOS severe environment, the distribution changes suddenly, stepwise model seems more adapted (suggested by Ifsttar): heuristic approach (Hutter identifier modified)

Focus: stepwise model identificat°

$\epsilon_R \epsilon_\theta$ error data sets obtained from real field tests

ϵ_R radius error

ϵ_θ angle error



Hutter identificat°
(Gaussian assumption)

p, m, σ

probability of step change, mean and std of the step height (Gaussian distribution)
std of the additive noise (Gaussian distribution)

Laplace parameters adjustment

μ, b, min, max

mean, b parameter and limits of the step height (truncated Laplace distribution)

Cauchy parameters adjustment

x_0, γ, min, max

mode, scale parameter and limits of the additive integrated noise (truncated Cauchy distribution)

Cauchy parameters adjustment

x_0, γ, min, max

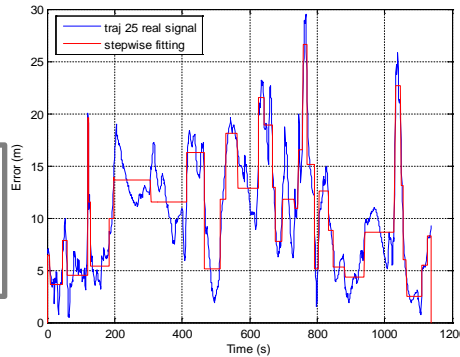
mode, scale parameter and limits of the angle random walk (truncated Cauchy distribution)



Focus: stepwise model identificat°

$\epsilon_R \ \epsilon_\theta$ error data sets obtained from real field tests

ϵ_R radius error



p, m, σ

probability of step change, mean and std of the step height (Gaussian distribution)

ARMAX filter identificat°



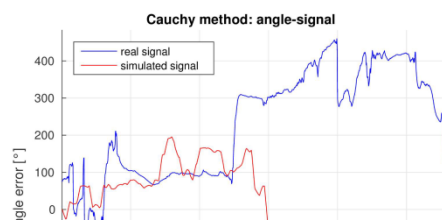
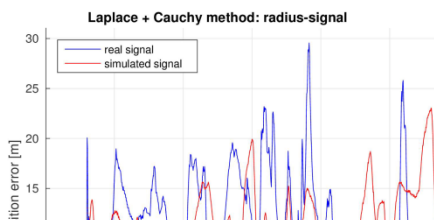
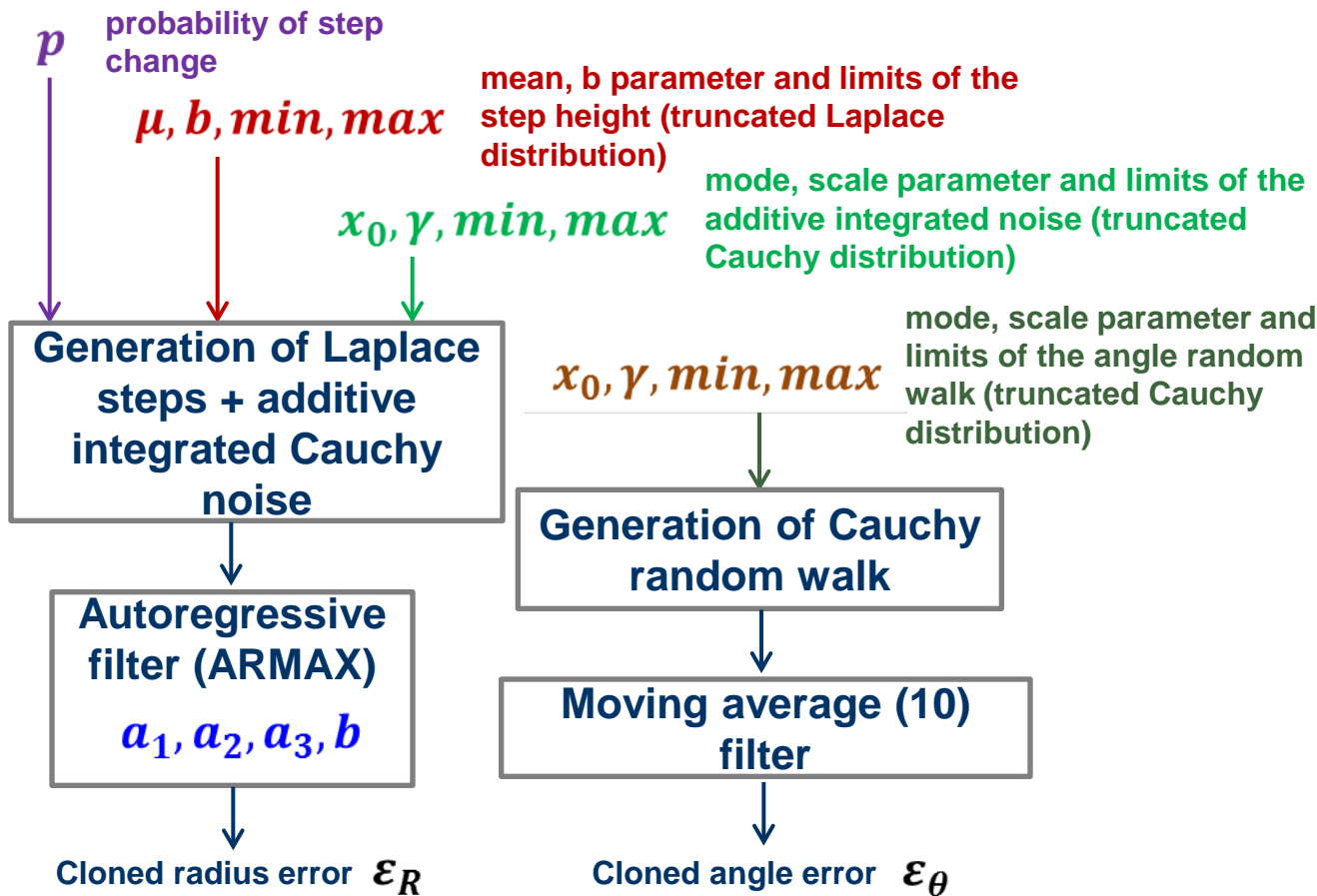
a_1, a_2, a_3, b

parameters of the ARMAX filter for smoothing



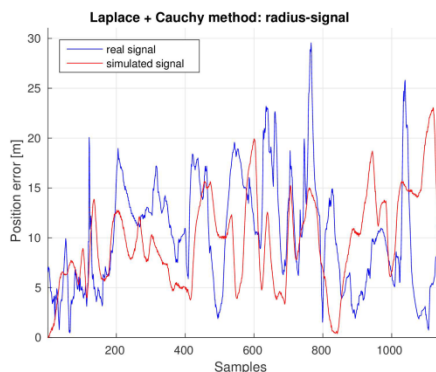
COST is supported by the EU Framework Programme Horizon 2020

Random cloned trajectory generat^o

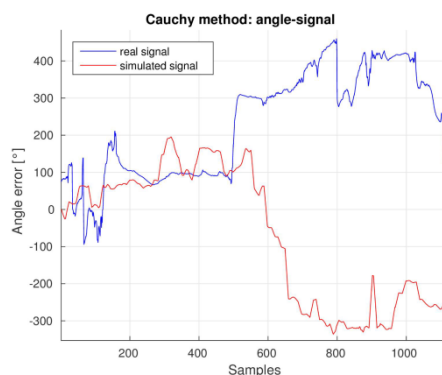


Random cloned trajectory generat^o

Cloned radius error ϵ_R



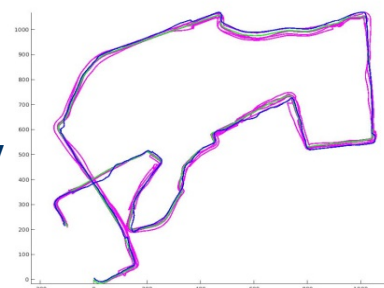
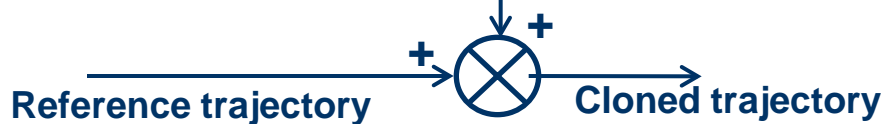
Cloned angle error ϵ_θ



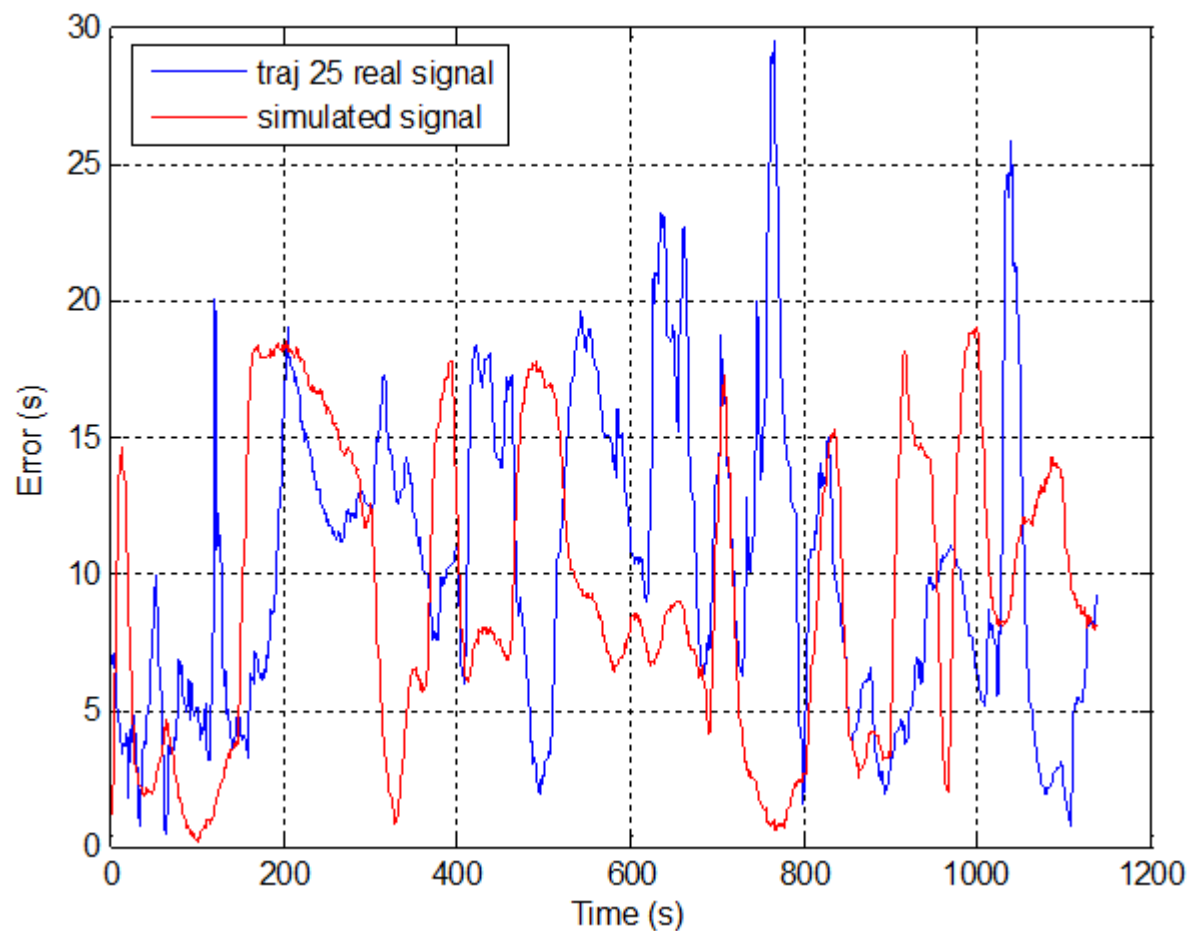
Polar to Cartesian

$$\begin{cases} \epsilon_X[n] = \epsilon_R[n] \cdot \cos(\epsilon_\theta[n]) \\ \epsilon_Y[n] = \epsilon_R[n] \cdot \sin(\epsilon_\theta[n]) \end{cases}$$

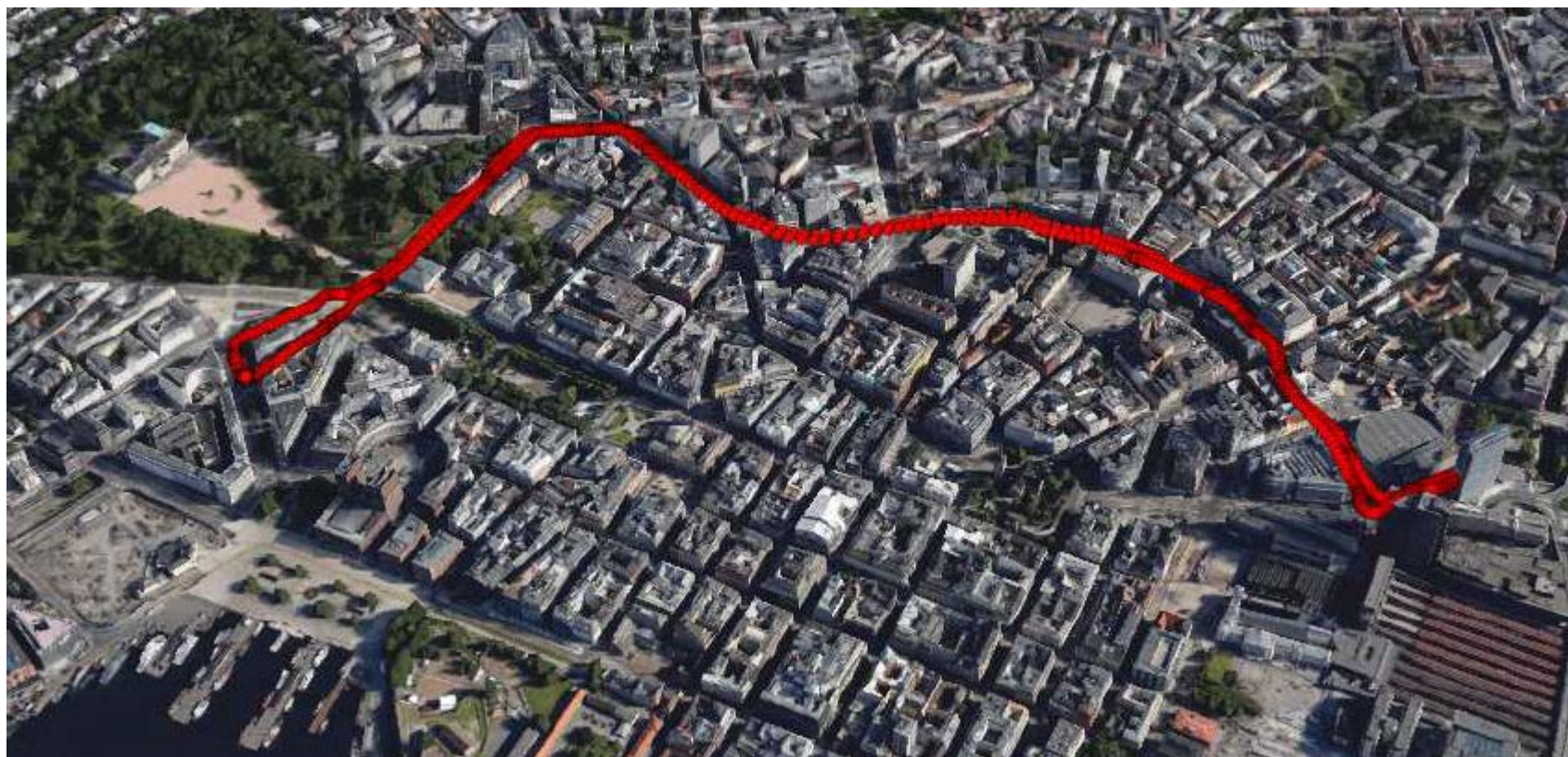
ϵ_X, ϵ_Y



Ex. of error clone (step model)



Reference traj in Oslo



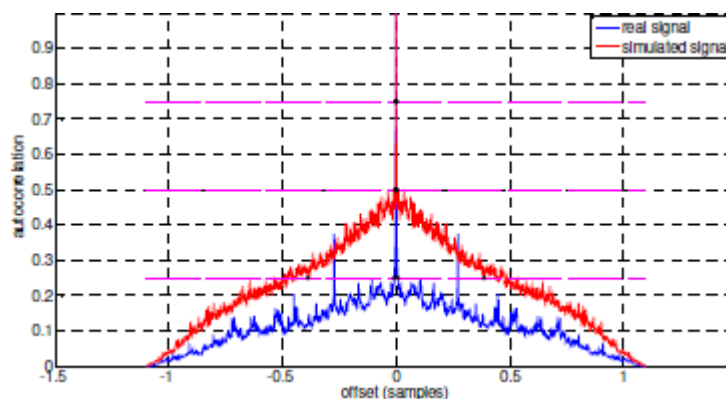
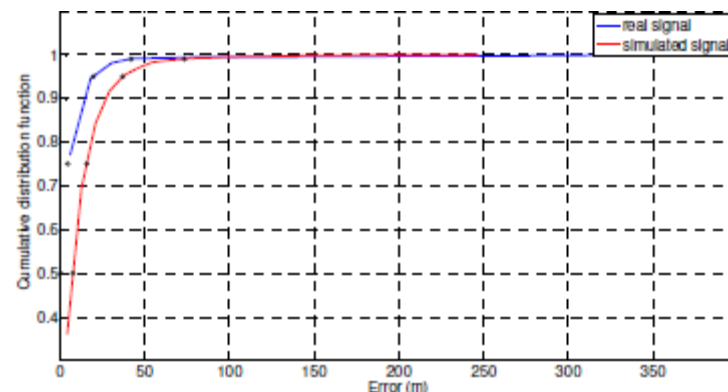
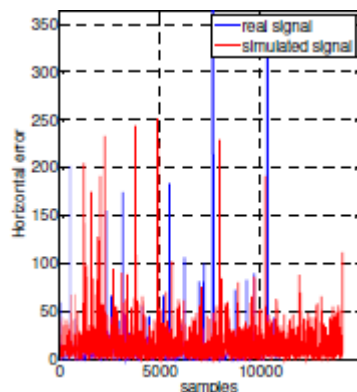
Clones in Oslo (AR model)



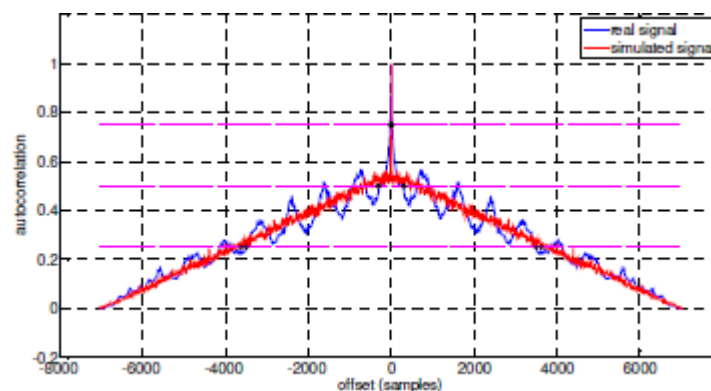
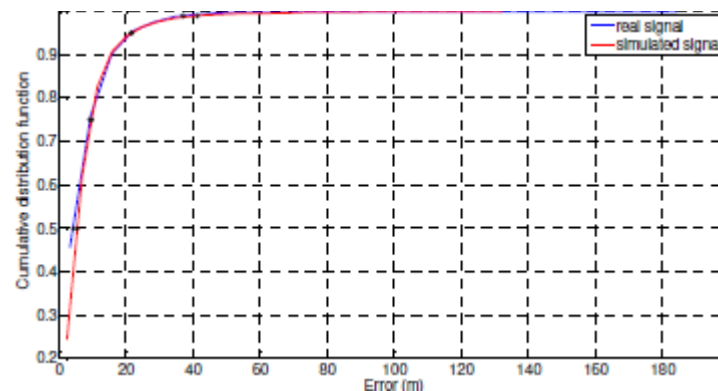
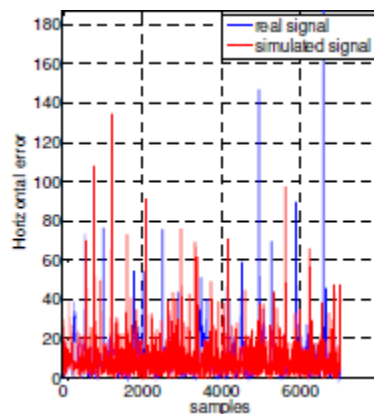
Validation

- A neural network validation tool is under development at Telespazio (GP-Start pj)
- Measuring the similarity of a generated signal with a signal data set vs different criteria:
 - time/frequency domains
 - distribution
 - autocorrelation

Example of a non-similar err. clone



Example of similar err. clone



Conclusions

- AR model (by Telespazio) versus Laplace-steps and Cauchy-random walk mixing model (by Ifsttar): model complexity and tuning vary from one environment to an other
- Validation based on autocorrelation and cdf seems promising
- Still a research question but progress have been made with extensive simulation of Road User Charging algorithm with QFree

THANK YOU FOR YOUR ATTENTION !

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